Functional Programming in Python

Problem

Write a program that counts the number of numbers in the range 0 through 1000 that contain the digit 7.

- The program in its entirety:

```
def containsSeven(s):
    return "7" in s

print len(filter(containsSeven, map(str, range(0, 1001))))
```

Functional Programming

- *Functional programming* is a programming paradigm that treats computation as the evaluation of mathematical functions.

- Programming languages that do not use this style are called imperative programming languages (C, C++, Java, etc).

- For our purposes in this course, functional programming amounts to *passing functions as arguments to other functions*.

- We will learn about built-in Python functions `map`, `filter`, and `reduce` that are extremely powerful because they take other functions as arguments.

Functional Programming

- In general, it is easier to reason formally about programs written in functional programming style.

- **General purpose functional programming languages**: Lisp, Scheme, Haskell, OCaml, etc.
- **Specialized functional programming languages**: Mathematica (mathematical computation), R (statistical computation), etc.

- Python has elements of both imperative style and functional style.

The map function

- map(f, [a, b, c, d, e]) returns the list [f(a), f(b), f(c), f(d), f(e)]
- The first argument of map is a function f and the second argument is a list L; it returns a new list obtained by applying f onto every element of L.

Examples:

- map(round, [4.57, -9.876, math.pi]) returns [5.0, -10.0, 3.0]
- map(str, range(0, 6)) returns ['0', '1', '2', '3', '4', '5']

- The map function allows us to construct new lists from old ones.

The map function

- Note that one can equivalently use the for-loop or the while-loop. Using the map function is faster.
- The map function can also take functions with more than one argument.

Example:

```
def pow(x, y):
    return x + y
>>> map(pow, [3, 4, 5], [5, 6, 7])
[8, 10, 12]
```

The filter function

- filter(f, L) returns a sublist of L consisting of those elements in L (in the same order as they appear in L) for which the boolean function f evaluates to True.

- **Examples:**
  - filter(bool, [0, -10, 0.0, None, "hello"]) returns [-10, 'hello']

  - filter(containsSeven, map(str, range(1001))) returns a list containing all of the numbers in the range 0 through 1000 that contain 7.

The reduce function

- This function is used as:

$$reduce(f, L)$$

- Here f is a two-argument function and L is a list.

- At each step, reduce passes the current answer along with the next item from the list, to f. By default, the first item in the sequence initialized the starting value.

Example: reduce(multiply, range(1, n+1)) is a compact and efficient way of computing n!.