

Jan 28, 2005 -- Lecture 5



22C:169

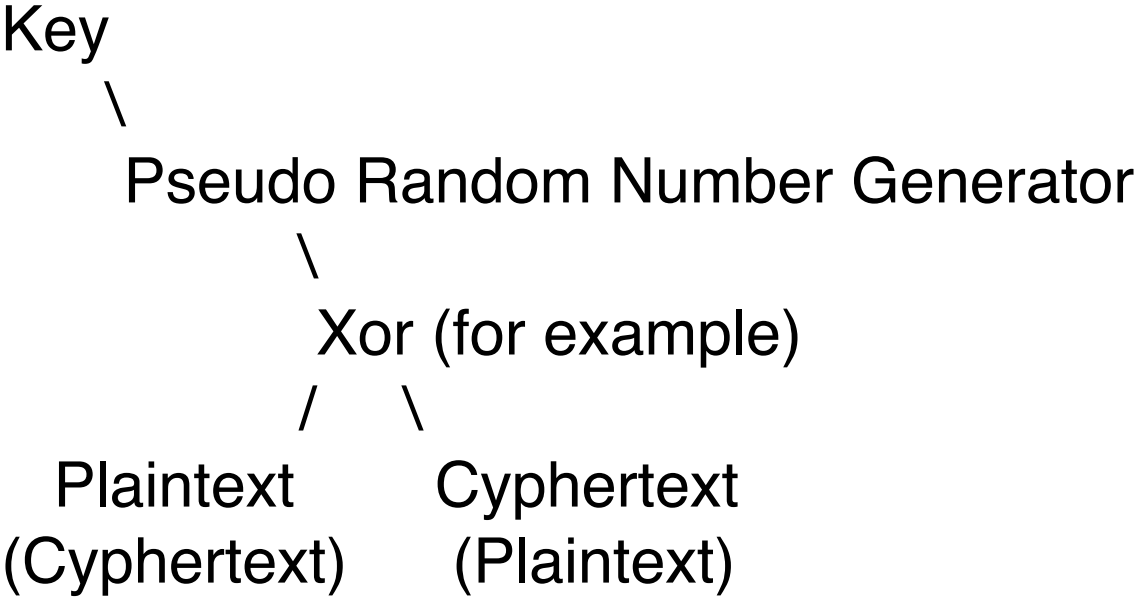
# Computer Security

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Stream Cyphers

# An Idea For Symmetric Key Cyphers



# Pseudo Random Number Generation

Not obviously possible --

*Computers are deterministic*

Properties:

$S_1 = \text{seed}$  (used as cryptographic key)

$S_n = f(S_{n-1})$  (must be one to one)

$R_n = g(S_n)$  (may be many to one)

$S_n = S_{n+p}$  ( $p$  is a period of  $f$ )

Seed is small and portable

Stream  $K$  is arbitrary length

## Linear Congruential PRNG (RANDU)

$$S_n = (k S_{n-1}) \bmod (2^{31})$$

$$k = 65,539$$

This horrible PRNG lives on, despite the fact that it is awful, failing many obvious tests for randomness!

# Linear Congruential PRNG

$$S_n = (k S_{n-1}) \bmod (2^{31} - 1)$$

$$k = 16,807 \text{ or } 48,271 \text{ or } 69,621$$

Period of the Generator

$$S_n = S_{n+2^{31}-2}$$

Source

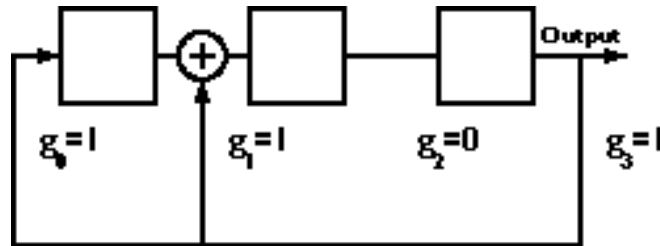
Park and Miller, *CACM*, 31, 10 (Oct 1988)

Random number generators --

Good ones are hard to find

# Linear Feedback Shift Registers

Shift register with XORed feedback:



Period, in bits, is  $2^n - 1$  for an  $n$  bit register, *but only if the taps are in the right places!*

```
Sn = if odd(Sn-1)  
      then (Sn-1 >> 1) ⊕ mask  
      else  Sn-1 >> 1
```

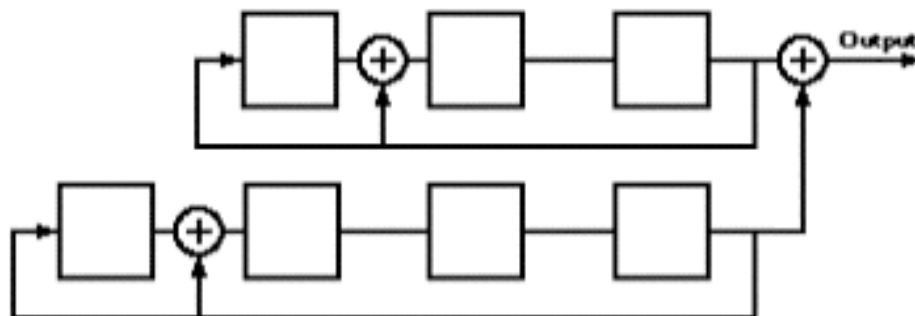
```
Rn = Sn mod 2
```

## Combine weak PRNGs to make Strong?

$Seed_{\text{COMBINED}} = Seed_1 \parallel Seed_2$  ?

Weak combining function and

$Period_1 \neq Period_2$



Entering Dangerous Territory!

## Combine weak PRNGs to make Strong?

$Seed_{\text{COMBINED}} = Seed_1 \parallel Seed_2$  ?

Selective combining function and

$Period_1 = Period_2$

$S_n = \langle S_{1n}, S_{2j}, S_{3k} \rangle$

$S_{n+1} = \text{if even}(S_{1n})$

**then**  $\langle S_{1n+1}, S_{2j+1}, S_{3k} \rangle$

**else**  $\langle S_{1n+1}, S_{2j}, S_{3k+1} \rangle$

$R_n = \text{if even}(S_{1n}) \text{ then } S_{2j} \text{ else } S_{3k}$

Entering Dangerous Territory!



# ISAAC

*Indirect, shift, accumulate and count*

Robert Jenkins, 1996

Seed: 256 integers, 32 bits each

Period:  $2^{8295}$

Must search  $4.67 \times 10^{1240}$  initial states  
for attack (square root of all possible).

Marina Pudovkina, 2001

A Known Plaintext Attack on the ISAAC ...

## Seeding PRNGs

- I. Use the text of the cryptographic key.  
*keys must be small enough to carry*
- II. Seed with a genuine random number.  
*must share number with remote user*
- III. Use small key to send big random key  
*requires source of real randomness*

A Key Exchange Protocol

## How to Generate Genuine Randomness:

- I. Radioactive decay or cosmic rays  
*inter-event intervals are exponential*
- II. Arrival times of eg: keypresses  
*inter-event has no fixed distribution*
- III. Number of lines in system log file  
*ad-hoc, system dependent.*

Problem: *How many bits of randomness per second can we get from each source?*

## How to combine randomness?

$B_1$  = random bits from source 1

$B_2$  = random bits from source 2

*sources must be independent*

$B_1 \parallel B_2$  -- concatenation

*risks loss of  $B_1$  if mod  $2^n$*

$B_1 \times B_2$  -- multiplication

*does not produce prime results*

Be Very Careful