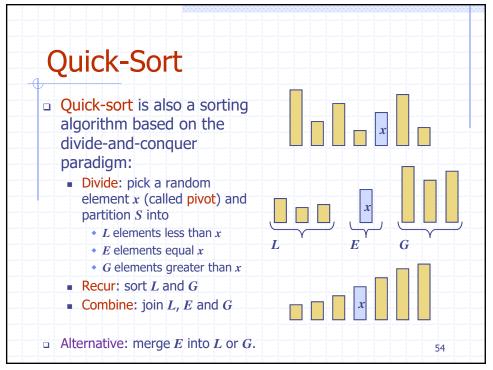
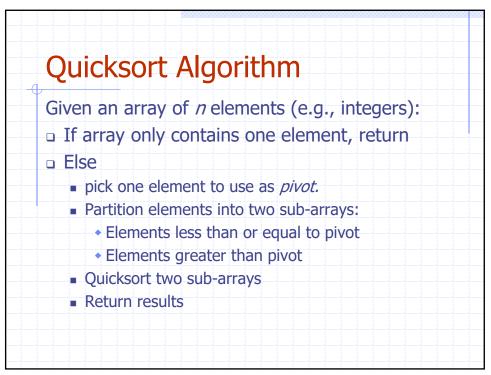
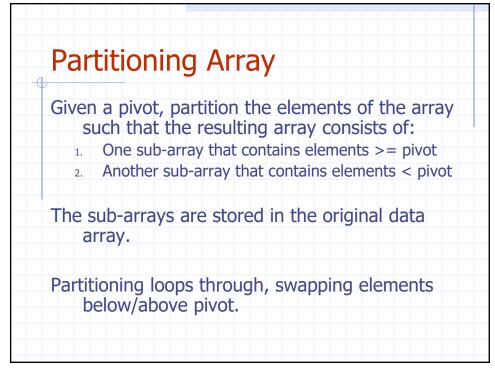


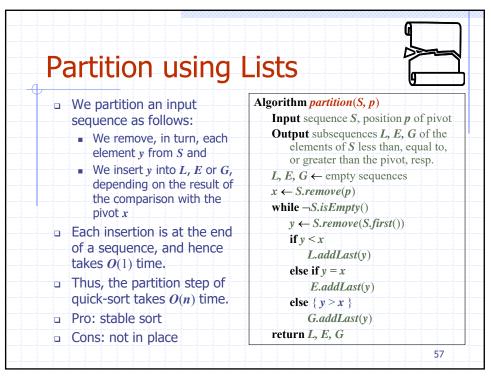
	Number of	Pds	ses		xtern	dl 20	ſĹ	
- - -	gain of utilizin	g all a	availal	ble bu	ffers			
	importance of	a hig	h fan-	in duri	ing me	rging		
	#Buffers available in main-memory							
	N	B=3	B=5	B=9	B=17	B=129	B=257	
	100	7	4	3	2	1	1	
	1,000	10	5	4	3	2	2	
	10,000	13	7	5	4	2	2	
Pages	100,000	17	9	6	5	3	3	
in File	1,000,000	20	10	7	5	3	3	
	10,000,000	23	12	8	6	4	3	
	100,000,000	26	14	9	7	4	4	
	1,000,000,000	30	15	10	8	5	4	

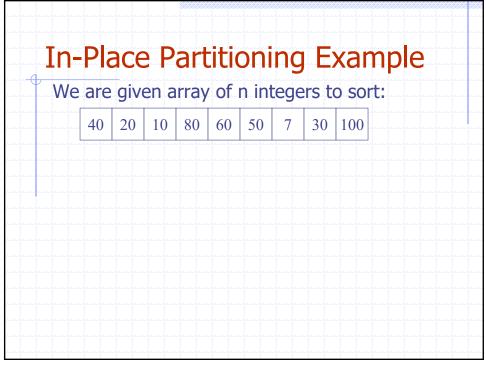
Summary of Sorting Algorithms							
Algorithm	Time	Notes					
selection-sort	O (n ²)	 stable in-place for small data sets (< 1K) 					
insertion-sort	O (n ²)	 stable in-place for small data sets (< 1K) 					
heap-sort	O (n log n)	 non-stable in-place for large data sets (1K — 1M) 					
merge-sort	O (n log n)	 stable sequential data access for huge data sets (> 1M) 					

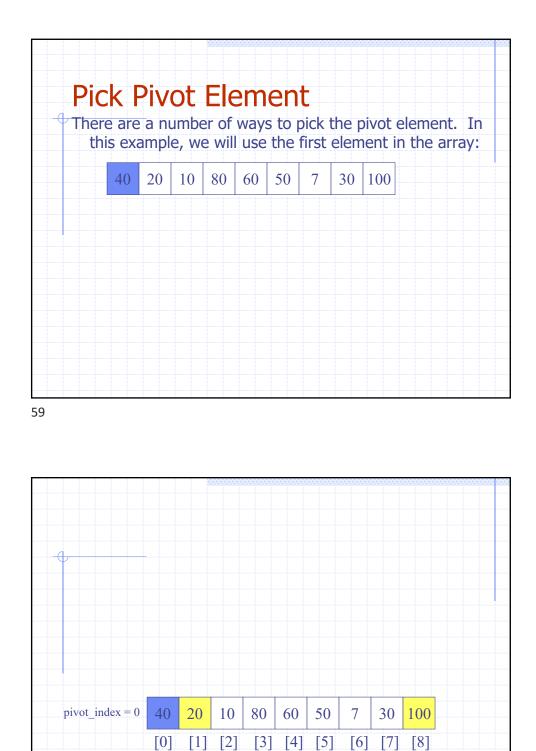






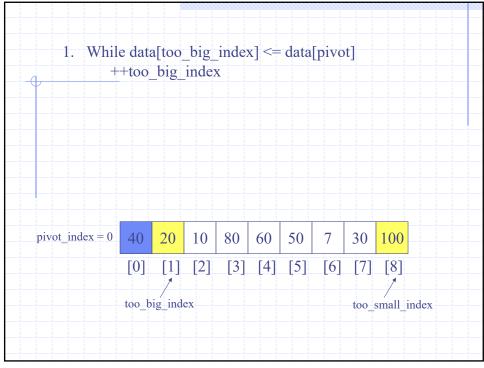


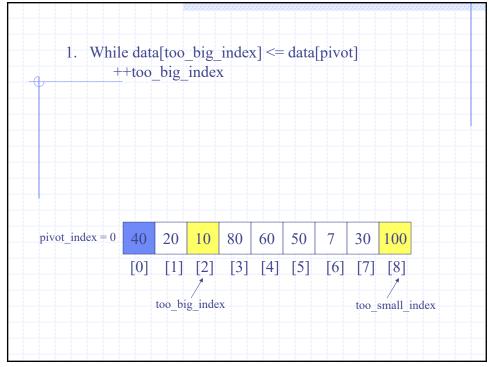


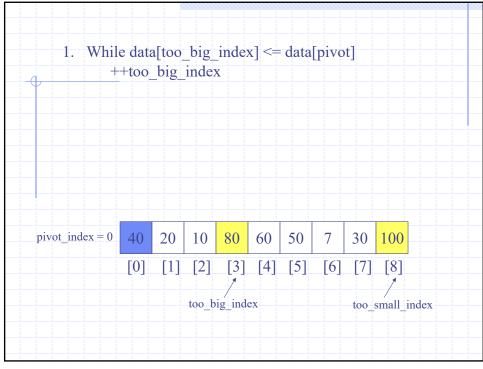


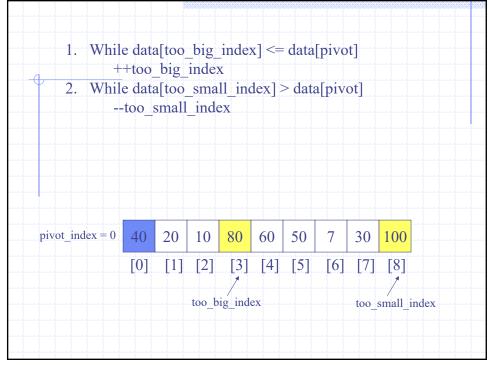
too_small_index

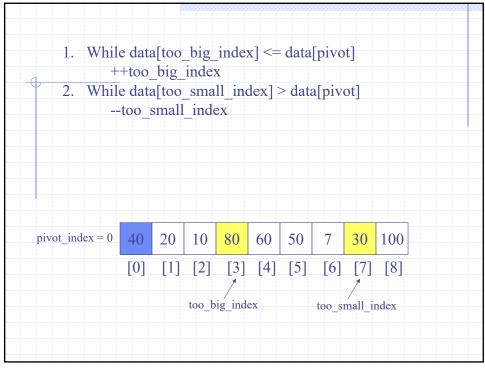
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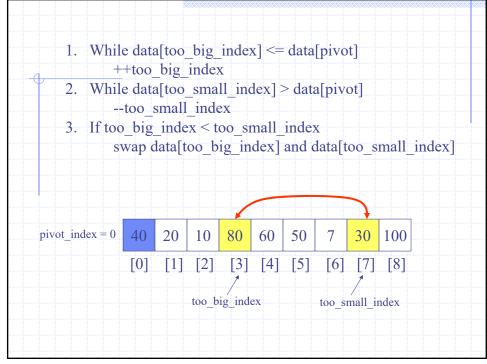


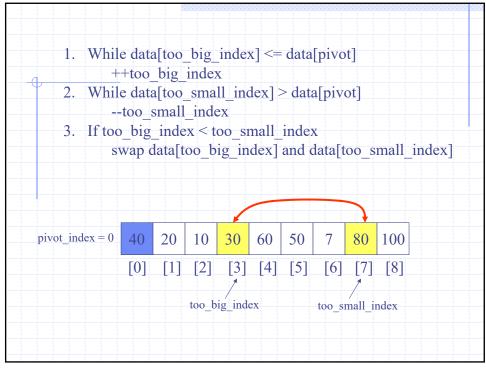


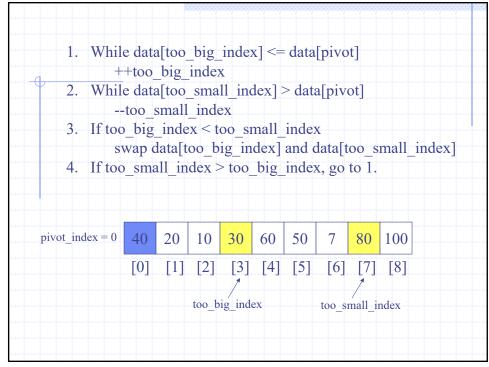


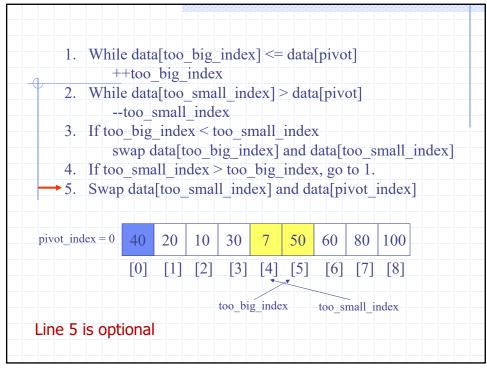


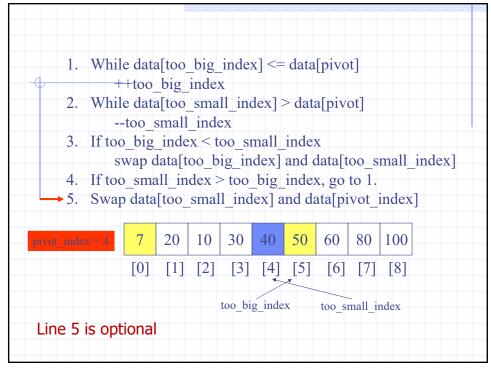


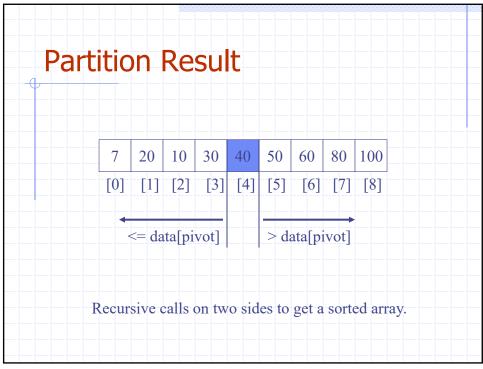


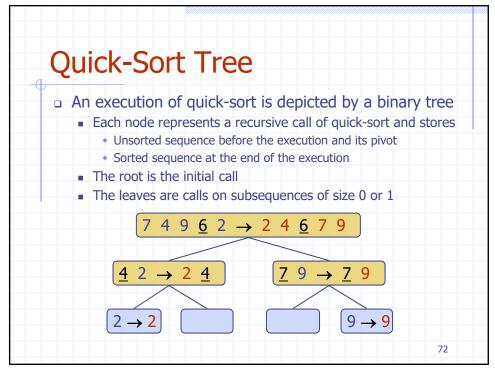


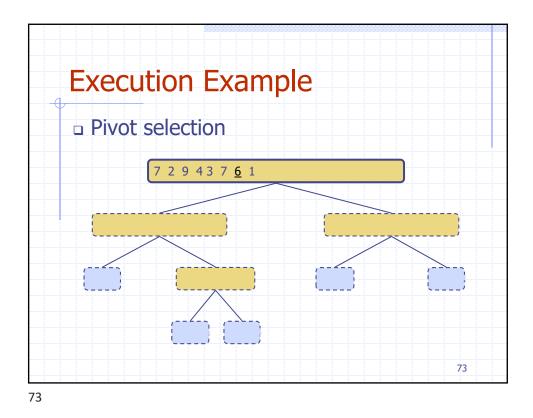


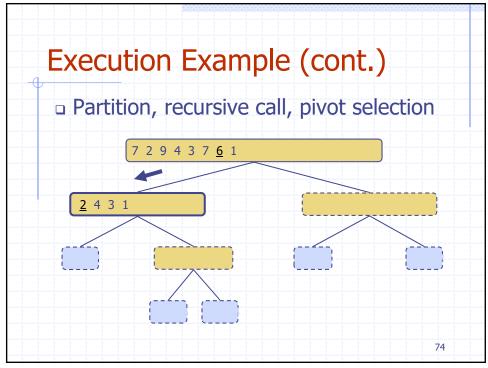


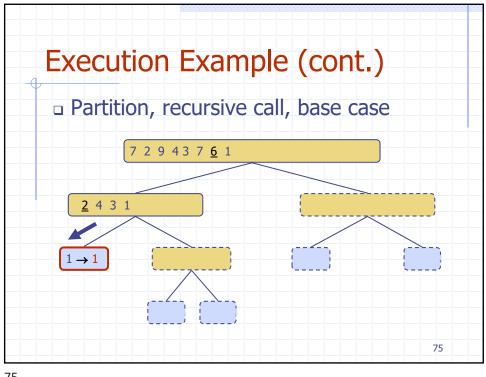


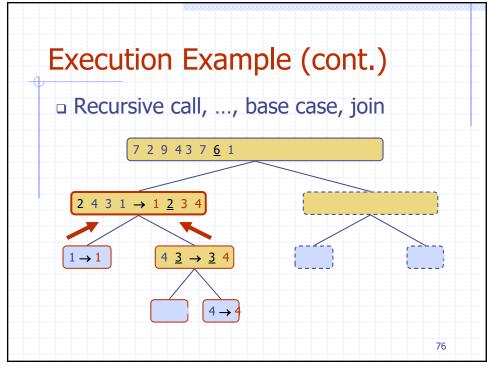


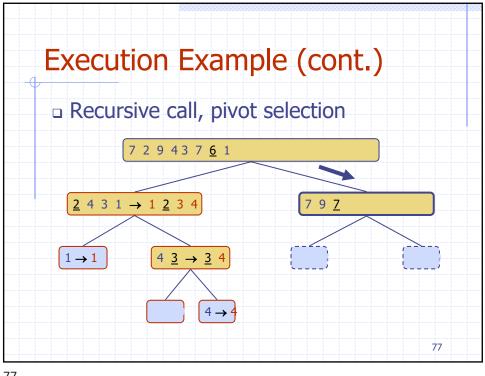


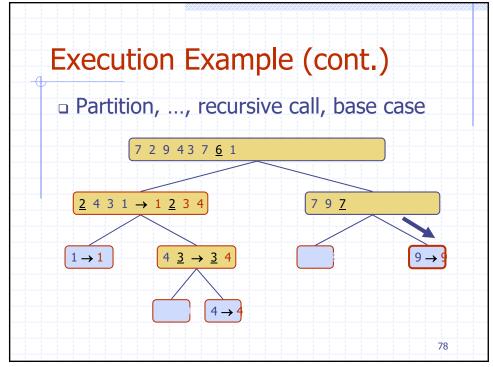


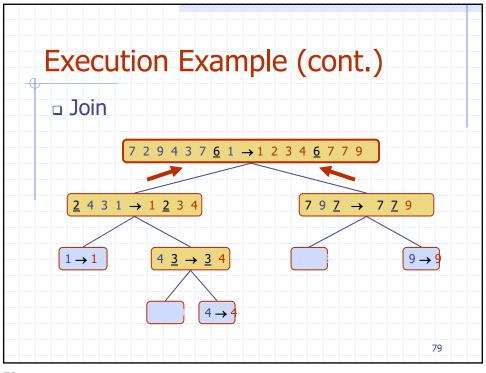


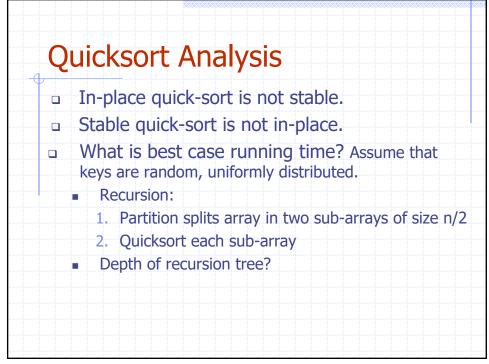


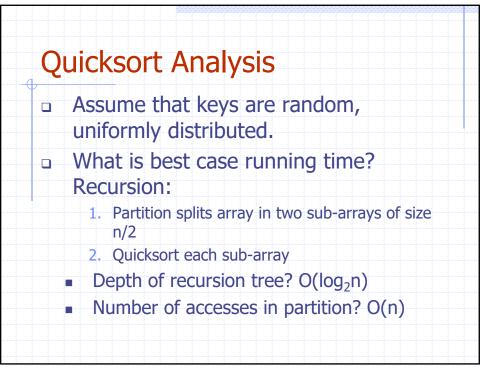


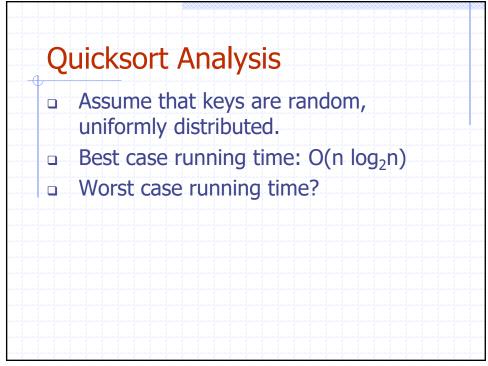


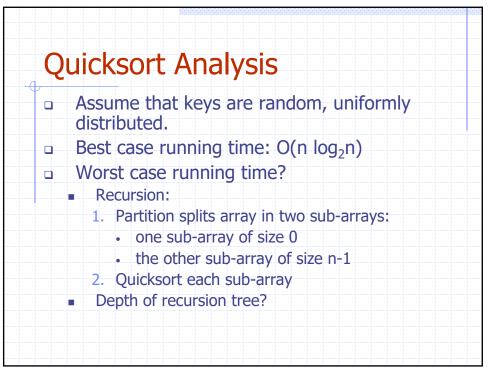


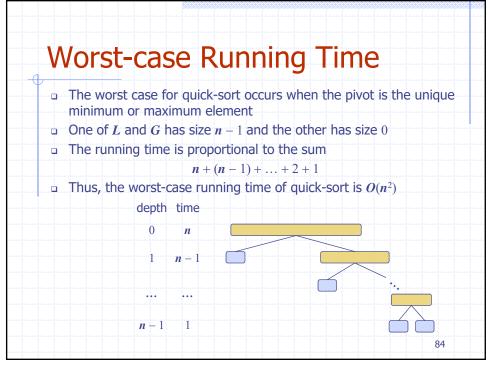


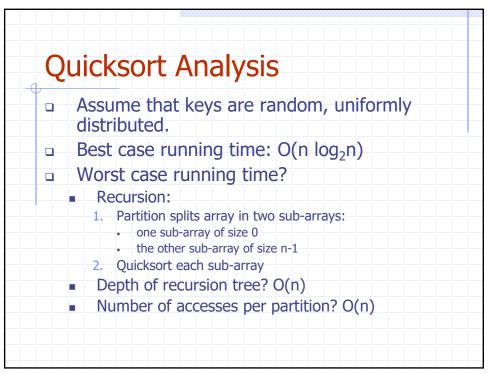


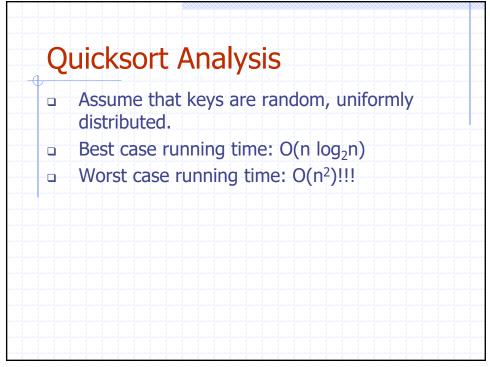


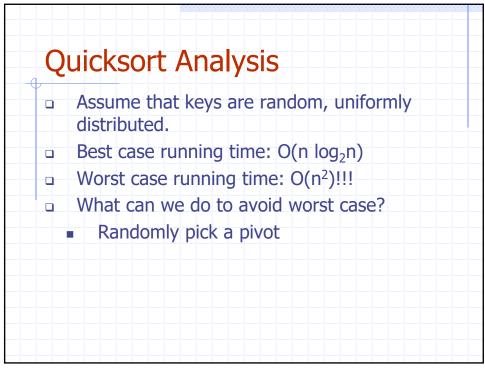


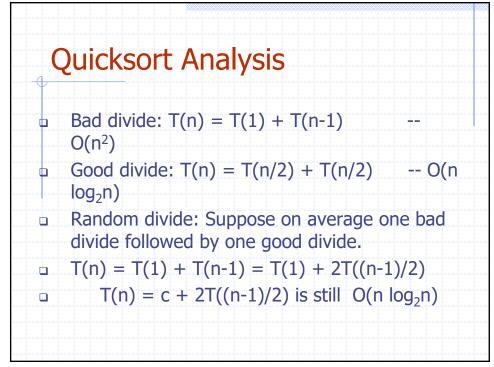


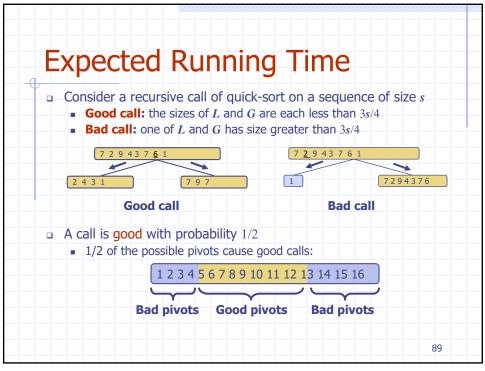


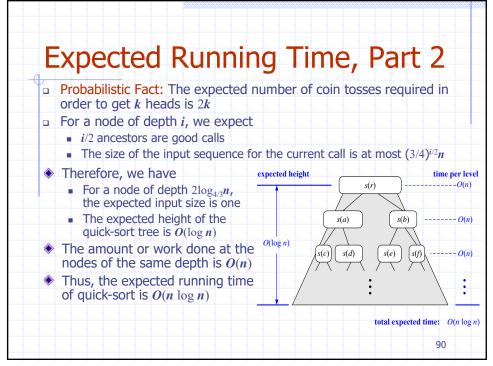




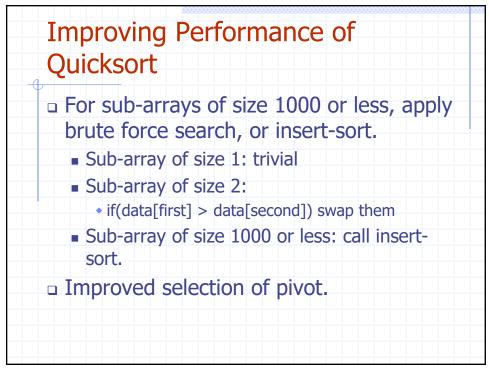


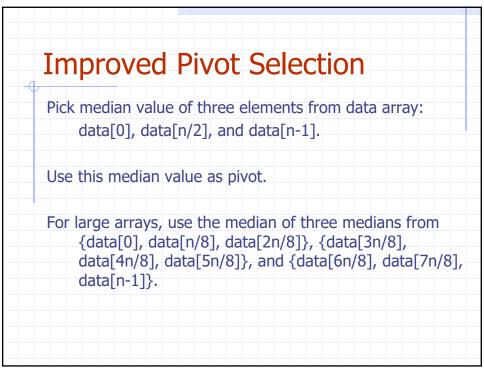


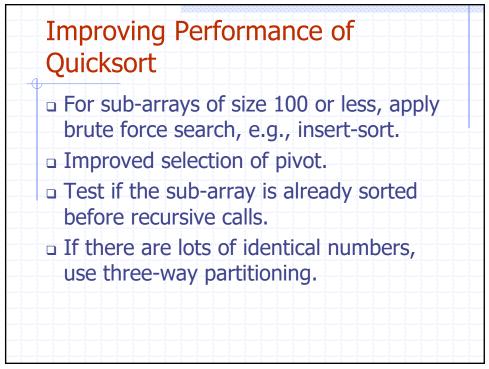


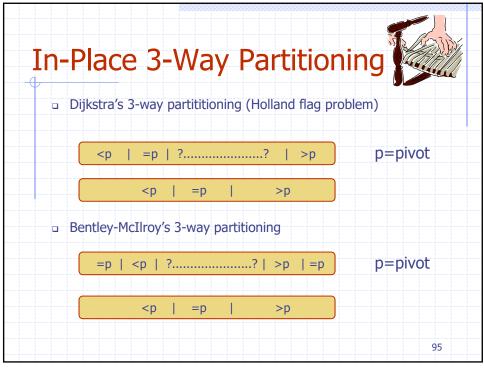


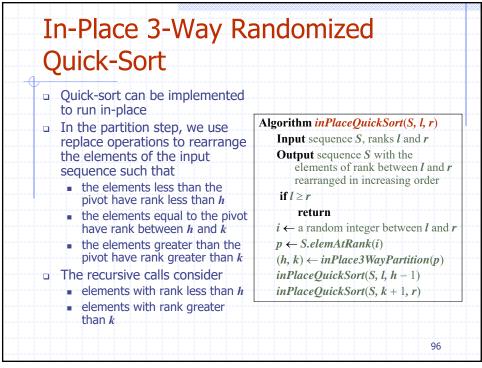








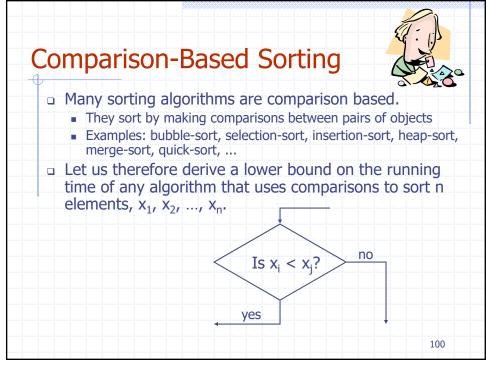


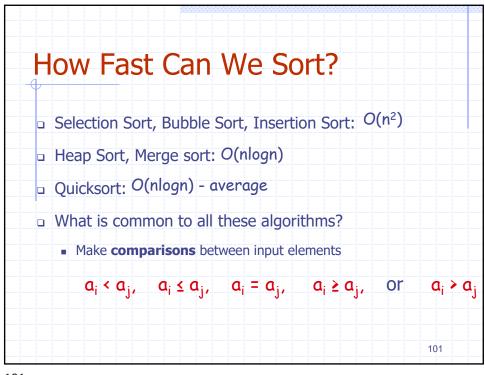


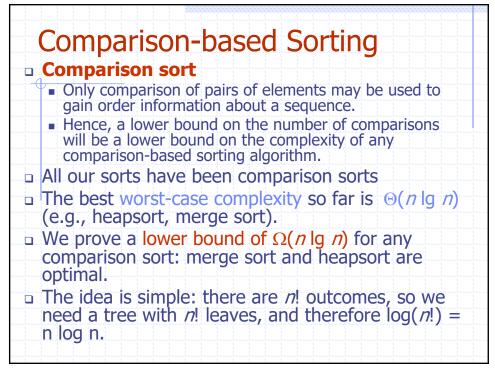
Stability of s	ortin	n	al	aorith	ms
Jean of a		3	<u> </u>	901101	
		1			
A STABLE sort pre	eserves re	elati	ve	order of re	cords with
equal keys					
equal neys)))))	.)))))
	Aaron	4	A	664-480-0023	097 Little
Sorted on first key:	Andrews	3	A	874-088-1212	121 Whitman
	Battle	4	С	991-878-4944	308 Blair
	Chen	2	A	884-232-5341	11 Dickinson
	Fox	1	A	243-456-9091	101 Brown
	Furia	3	A	766-093-9873	22 Brown
	Gazsi	4	в	665-303-0266	113 Walker
	Kanaga	3	в	898-122-9643	343 Forbes
	Rohde	3	A	232-343-5555	115 Holder
	Quilici	1	С	343-987-5642	32 McCosh
Sort the first file on					
second key:	Fox	1	A	243-456-9091	101 Brown
	Quilici	1	С	343-987-5642	32 McCosh
Records with key value	Chen	2	A	884-232-5341	11 Dickinson
	Kanaga	3	в	898-122-9643	343 Forbes
3 are not in order on	Andrews	3	A	874-088-1212	121 Whitman
first key!!	Furia	3	A	766-093-9873	22 Brown
	Rohde	3	A	232-343-5555	115 Holder
	Battle	4	С	991-878-4944	308 Blair
	Gazsi	4	в	665-303-0266	113 Walker
	Aaron	4	A	664-480-0023	097 Little

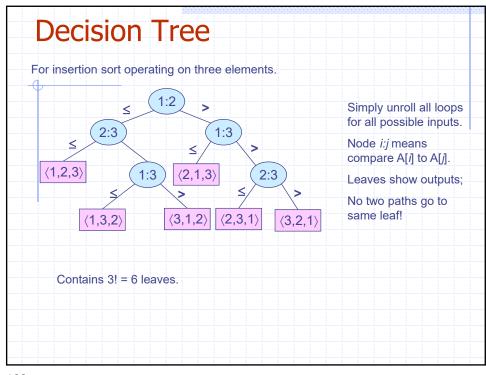
Algorithm	Time	Notes	
selection-sort	O (n ²)	in-place, stableslow (not good for any inputs)	
insertion-sort	O (n ²)	in-place, stableslow (good for small inputs)	
quick-sort	O(n log n) expected	 in-place, not stable fastest (good for large inputs) 	
heap-sort	O (n log n)	 in-place, not stable fast (good for large inputs) 	
merge-sort	O (n log n)	 not in-place, stable fast (good for huge inputs) 	

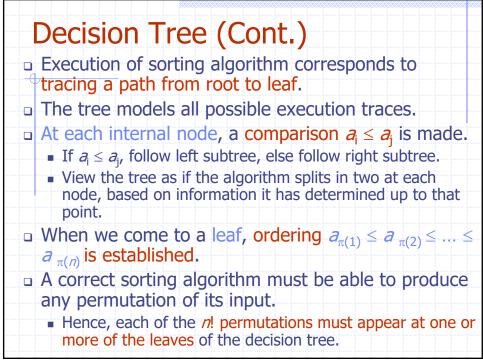
	Simple Divide	Fancy Divide	
Uneven Divide 1 vs n-1	Insert Sort	Selection Sort	
Even Divide n/2 vs n/2	Merge Sort	Quick Sort	

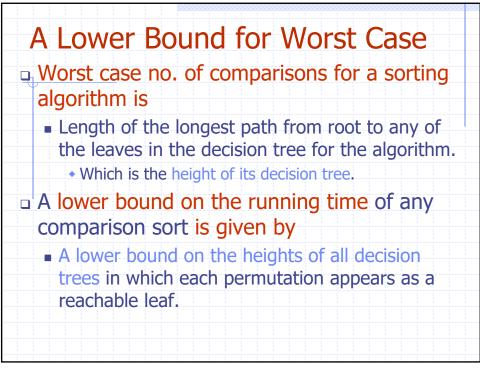


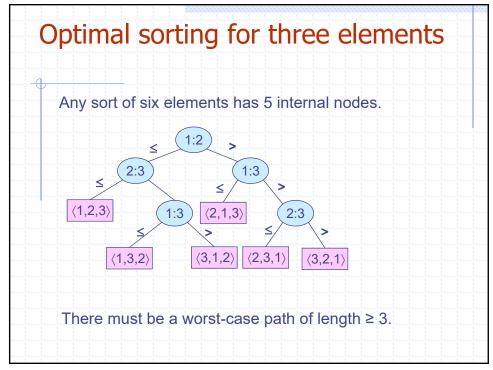


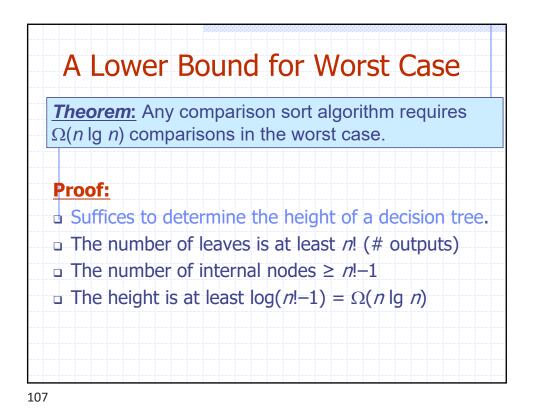


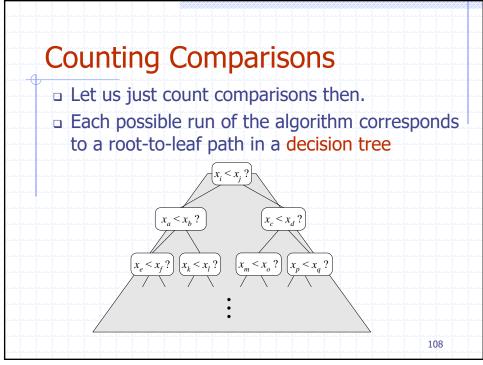


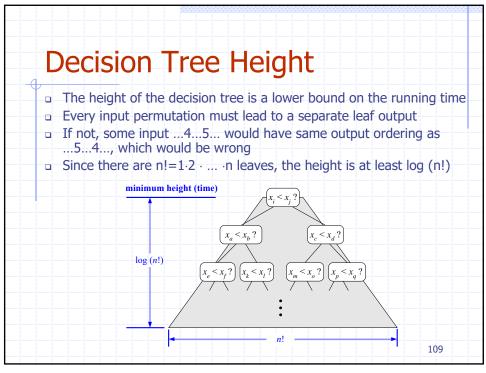












The Lower Bound • Any comparison-based sorting algorithms takes at least log(n!) time • Therefore, any such algorithm takes worst-case time at least $\log(n!) \ge \log\left(\frac{n}{2}\right)^{\frac{n}{2}} = (n/2)\log(n/2).$ • That is, any comparison-based sorting algorithm must run in $\Omega(n \log n)$ time in the worst case.