

### Sobel Filtering:

Sobel filtering is a *three step* process. Two  $3 \times 3$  filters (often called *kernels*) are applied separately and independently. The weights these kernels apply to pixels in the  $3 \times 3$  region are depicted below:

-1	0	+1
-2	0	+2
-1	0	+1

+1	+2	+1
0	0	0
-1	-2	-1

Again, notice that in both cases, the sum of the weights is 0. The idea behind these two filters is to approximate the derivatives in  $x$  and  $y$ , respectively. Call the results of these two filters  $D_x(x, y)$  and  $D_y(x, y)$ . Both  $D_x$  and  $D_y$  can have positive or negative values, so you need to add 0.5 so that a value of 0 corresponds to a middle gray in order to avoid clamping (to  $[0..1]$ ) of these intermediate results.

The final step in the Sobel filter approximates the gradient magnitude based on the partial derivatives ( $D_x(x, y)$  and  $D_y(x, y)$ ) from the previous steps. The gradient magnitude, which is the result of the Sobel Filter  $S(x, y)$ , is simply:

$$S(x, y) = \sqrt{(D_x(x, y))^2 + (D_y(x, y))^2} \quad (1)$$

Please note that your textures should not store  $D_x(x, y)$ , but should rather store  $D_x(x, y) + 0.5$ , as I mentioned above... This means before computing the value in Equation 1, you need to first subtract the 0.5 you added when computing  $D_x$  and  $D_y$ !

So, in summary, the three steps are:

- Compute the image storing partial derivatives in  $x$  ( $D_x(x, y)$ ) by applying the right  $3 \times 3$  kernel to the *original* input image.
- Compute the image storing partial derivatives in  $y$  ( $D_y(x, y)$ ) by applying the left  $3 \times 3$  kernel to the *original* input image.
- Compute the gradient magnitude  $S(x, y)$  based on  $D_x$  and  $D_y$ .

Two further things to notice about Sobel filters: (a) both the derivative kernels depicted above are separable, so they could be split into disjoint  $x$  and  $y$  passes, and (b) the entire filter can actually be implemented in a single-pass GLSL filter in a relatively straightforward manner.