

The First Programming Problem



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Problem: Converting decimal numbers to binary



- Given a non-negative integer, convert it into its **binary equivalent**.
- **Example:**
 - **Input:** 123 **Output:** 1111011
 - **Input:** 1363 **Output:** 10101010011
 - **Input:** 12 **Output:** 1100

Plan of Action



1. Understand the problem. What does “binary equivalent” mean?
2. Design algorithms for the problem. How would we solve the problem with a pencil and paper?
3. Write down pseudocode for the algorithm.
4. Translate the pseudocode to Python code.
5. Test, test, test.

This example will illustrate



- Constants
- Variables
- Operators
- Data types
- Expressions
- Function calls
- Input statements
- Output statements
- Control flow statements

Decimal numbers revisited



Consider the decimal number 8,374.

8	3	7	4
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Place value 1000 100 10 1

Therefore, the “value” of this number is

$$8 \times 1000 + 3 \times 100 + 7 \times 10 + 4 \times 1$$

What are binary numbers?



Similarly, consider the binary number 10110110.

1	0	1	1	0	1	1	0
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Place values: 128 64 32 16 8 4 2 1

Just like the place values for decimal numbers are powers of 10, the place values for binary numbers are powers of 2.

Therefore, the “value” of this number is

$$128 + 32 + 16 + 4 + 2 = 182$$

Table of Binary Equivalents



Decimal	Binary
0	0
1	1
2	10
3	11
4	100
5	101
6	110
7	111
8	1000
9	1001
10	1010
11	1011
12	1100

Two observations based on this table



Observation 1:

If n is even, then its binary equivalent ends with a 0; otherwise if n is odd, its binary equivalent ends with 1.

Two observations based on the table



Observation 2:

Suppose that the binary equivalent of n is

$$b_k \dots b_2 b_1 b_0$$

If n is even, then the binary equivalent of $n/2$ is

$$b_k \dots b_2 b_1$$

and if n is odd, then the binary equivalent of $(n-1)/2$ is

$$b_k \dots b_2 b_1$$

This suggests an algorithm



- Check if the given number n is odd or even.
- If n is even, we know that its binary equivalent ends with 0. Furthermore, to get the rest of n 's binary equivalent, we need to “consult” $n/2$.
- If n is odd, we know that the binary equivalent ends with 1. Furthermore, to get the rest of n 's binary equivalent, we need to “consult” $(n-1)/2$.

Illustration of this algorithm



Let the given input be $n = 203$.

1. $n = 203$ is odd. So rightmost bit is 1.

To get the rest of the answer we should “consult” $(n-1)/2 = 101$.

2. $n = 101$ is odd. So the rightmost bit is 1.

To get the rest of the answer we should “consult” $(n-1)/2 = 50$

3. $n = 50$ is even. So the rightmost bit is 0.

To get the rest of the answer we should “consult” $n/2 = 25$.

4. $n = 25$ is odd. So the rightmost bit is 1.

To get the rest of the answer we should “consult” $(n-1)/2 = 12$.

5. $n = 12$ is even. So the rightmost bit is 0.

To get the rest of the answer we should “consult” $n/2 = 6$.

6. $n = 6$ is even. So the rightmost bit is 0.

To get the rest of the answer we should “consult” $n/2 = 3$.

7. $n = 3$ is odd. So the rightmost bit is 1.

To get the rest of the answer we should “consult” $(n-1)/2 = 1$.

8. $n = 1$ is odd. So the rightmost bit is 1.

To get the rest of the answer we should “consult” $(n-1)/2 = 0$.

So the output (right to left) is **1 1 0 1 0 0 1 1**.

Pseudocode



1. Read the number n given as input.
2. If n is even, output 0. Replace n by $n/2$.
3. If n is odd, output 1. Replace n by $(n-1)/2$.
4. If n is 0, stop. Otherwise go to Line 2.

Note that this algorithm produces the binary equivalent of n in “right to left order.”

Our first program



```
n = int(raw_input("Enter a positive integer:"))  
while n > 0:  
    print n % 2  
    n = n/2
```